

Instructions: Upload LEGIBLE, COMPLETE solutions to Gradescope before 11:59pm on 8 December 2021.

1. Compute the tangent plane to the surface $\mathbf{s}(u, v) = \langle u + v, 3u^2, u - v \rangle$ at the point $(0, 3, -2)$.
2. Compute the surface area of the sphere of radius $\alpha > 0$ centered at the origin.
3. Compute the area of the part of the surface $z = xy$ which lies inside the cylinder $x^2 + y^2 = 9$.
4. Compute $\iint_S y^2 z^2 \, dS$ for the part of the sphere $x^2 + y^2 + z^2 = 4$ above the cone $z = \sqrt{x^2 + y^2}$.
5. Compute the flux of $\text{curl}(\mathbf{v})$ across the surface $z = x \sin(y)$ for $(x, y) \in [0, 2] \times [0, \pi]$ and $\mathbf{v} = \langle yz, zx, xy \rangle$.
6. Compute $\int_C \mathbf{v} \cdot d\mathbf{r}$ for $\mathbf{v} = \langle 1, x + yz, xy - \sqrt{z} \rangle$ where C is the boundary of the part of the plane $3x + 2y + z = 1$ in the first octant with orientation counterclockwise when viewed from above.
7. Compute the flux of $\mathbf{v} = \langle x^2 yz, xy^2 z, xyz^2 \rangle$ across the surface of the box $R = [0, 4] \times [0, 1] \times [-1, 2]$.
8. Compute $\iint_S (2x + 2y + z^2) \, dS$ for S the sphere of radius 2 centred at the origin.